# Problem 3: Bay Area's Railway Traversal 3 Points

Problem ID: crosstown Rank: 1

**Bounty: A CALICO Edition (Unofficial) BART** <u>Clipper Card</u> for the first team to solve any test set for this problem and fill out this <u>Google Form</u>!

#### Introduction

crosstown and subway form a two-part series with a similar setup! Be sure to check both out!

The year is <u>2038</u> and the <u>BART (Bay Area Rapid Transit)</u> is nearing completion of its long-awaited <u>Silicon Valley Extension</u>! They've also acquired <u>Caltrain</u>, and plan to create the <u>very first circular</u> train line in the Bay Area! Eager to see how things will be upon completion, <u>CALICO's Biggest</u> <u>Railfan</u> surveys members of the CALICO Team to CALICalculate some statistics. Which crosstown CALICommuters will be riding on the subway the longest?

#### **Problem Statement**

There is a circular subway loop with M stations numbered 1 to M. There are N passengers numbered 1 to N spread across these stations. Each passenger begins at their starting station  $S_1, S_2, \ldots, S_N$ , and needs to go to their ending station  $E_1, E_2, \ldots, E_N$ . To get there, they board a single subway that goes around the loop.

The stations are arranged clockwise on a circle by their numbers in ascending order. The subway begins at station 1 and travels clockwise, stopping at each station along the way. After stopping at station  $\mathbf{M}$ , it loops back to station 1.

At each station (including the initial station 1), passengers already on the subway whose  $E_i$  is the current station will exit the subway as they have arrived at their ending station. Next, passengers whose  $S_i$  is the current station will enter the subway. Then, the subway travels to the next station.

Each station is 1 mile apart. Find the longest distance traveled by any passenger when getting from their starting station to their ending station.

*Note: Templates are available for this problem—and* **all other problems in this contest**—in *Python, Java, and C++! Find them in the <u>contest.zip provided at the start of the contest</u>. Templates handle input and output for you, so you can just fill out a single function!* 

### **Input Format**

The first line of the input contains a single integer  $\mathbf{T}$  denoting the number of test cases that follow. For each test case:

- The first line contains two space-separated integers N M denoting the number of passengers and the number of stations.
- The second line contains N space-separated integers  $S_1 S_2 \dots S_N$ , denoting the starting station for each passenger in ascending order of passenger numbers.
- The third line contains N space-separated integers  $E_1 E_2 \dots E_N$ , denoting the ending station for each passenger in ascending order of passenger numbers.

# **Output Format**

For each test case, output a single line containing an integer denoting the longest distance traveled by any passenger when getting from their starting station to their ending station, in miles.

# Constraints

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1 \leq \mathbf{T} \leq 100

1 \leq \mathbf{S}_i, \mathbf{E}_i \leq \mathbf{M}

\mathbf{S}_i \neq \mathbf{E}_i

1 \leq \mathbf{N} \leq 10

2 \leq \mathbf{M} \leq 10
```

### Sample Test Cases

Sample Input								D	ownload	k	Sample Output				<u>Downloa</u>	<u>d</u>
6																
1	6										2					
3											4					
5											4					
1	6										4					
5	Ŭ										3					
3											6					
2	6															
1	4															
5	6															
2	8															
2	3															
6	5															
4	5															
1	3	3	5													
4	5	1	2													
7	7															
1	1	1	1	1	1	1										
7	7	7	7	7	7	7										

#### Sample Explanations

For test case #1, we have N = 1 passenger starting at station 3 who wants to get to station 5 in a loop with M = 6 stations. The subway travels to station 3, and the passenger enters. Then, the subway travels 2 miles to station 5, and the passenger exits. The passenger traveled 2 miles to get from their starting station to their ending station. Since there is only one passenger, the answer is 2. The path is illustrated below.



For test case #2, the situation is similar to test case #1 except the passenger starts at station 5 and ends at station 3. Since the subway is a loop, the passenger travels 4 miles in total:  $5 \rightarrow 6$ ,  $6 \rightarrow 1$ ,  $1 \rightarrow 2$ , and  $2 \rightarrow 3$ . Thus, the answer is 4. The path is illustrated below.



For test case #3, there are two passengers. The first passenger starts at station 1, ends at station 5, and travels 4 miles. The second passenger starts at station 4, ends at station 6, and travels 2 miles. Since the passenger who traveled 4 miles traveled further than the passenger who traveled 2 miles, the answer is 4. These two paths are illustrated below.



For test case #4, the passengers travel distances of 4 and 2. The longest is 4, so the answer is 4. For test case #5, the passengers travel distances of 3, 2, 3, 2. The longest is 3, so the answer is 3. For test case #6, all passengers have the same starting and ending stations and travel exactly 6 miles.