Problem 8: C1000001 10 Points

Problem ID: piano Rank: 3

Introduction

Billy the billion-tentacled octopus wants to perform some profound pieces at his upcoming piano recital! He'll be showcasing his custom built piano with a few "engineering" quirks.

Billy's piano has 1000000 octaves with 12000004 keys numbered from 1 to 12000004! In <u>scientific pitch notation</u>, key 1 plays A0, 2 plays A#0, 3 plays B0, 4 plays C1, ..., 40 plays C4 (middle C), ..., 49 plays A4 (A440), ..., and 12000004 plays C1000001 (which has such a high frequency it deatomizes air particles!).

With a billion tentacles, Billy can press as many notes as he needs simultaneously. Although the piano is long, he can instantly move to different parts of the piano when he isn't pressing down any keys. However, at any given point in time, he has limited reach! Help Billy determine what piece to play by finding the reach needed to play each piece!

Problem Statement

Given a piece of music with N timesteps involving a sequence of actions $A_i, A_2, ..., A_N$ and keys $K_i, K_2, ..., K_N$, where at timestep *i*, action A_i is taken with key K_i , find the reach needed to play the entire piece.

An action can involve either pressing or releasing a key.

The reach needed at a given timestep is equal to the maximum difference between any two currently pressed key numbers. The reach needed to play the entire piece is equal to the maximum reach needed at any single timestep.

All keys begin in the released state, and are pressed/released in the order of their respective timestep.

Input Format

The first line of the input contains a positive integer \mathbf{T} denoting the number of test cases that follow. For each test case:

- The first line contains an integer ${\bf N}$ denoting the number of timesteps in the piece
- The next N lines contain 2 space-separated values each $A_i K_i$, denoting actions and keys in the order they are played
 - $\circ~$ The single character A_i denotes the action to perform on key $K_i,$ and is one of the following:
 - P, denoting K_i is pressed at timestep *i*
 - R, denoting \mathbf{K}_{i} is released at timestep i
 - \circ The integer K_i denotes the key to take action A_i with
- The final line is blank to separate individual test cases

Output Format

For each test case, output a single line containing a positive integer denoting the reach needed to play the entire piece.

Problem Constraints

$$\begin{split} &1\leq T\leq 100\\ &2\leq N\leq 10^5\\ &\mathbf{N} \text{ is even.}\\ &\text{The sum of }\mathbf{N} \text{ across all test cases in an input does not exceed }10^5.\\ &1\leq K_i\leq 12\times 10^6+4=12000004\\ &\mathbf{A_i}\in\{\texttt{P},\texttt{R}\} \end{split}$$

The piece as a whole is additionally subject to the following constraints:

- All keys begin in the released state
- Every pressed key will be released by the end of the piece
- The same key may be pressed and released multiple times
- If a key is pressed, it will not be pressed again until it is released and vice versa

Sample Test Cases

Sample Input

Sample Output

Ρ	40 40 40 40)	0 31
10)		
Ρ	47	1	
Ρ	32		
Ρ	20)	
R	47	1	
Ρ	44	L	
R	44	L	
Ρ	51		
R	51		
R	32		

R 20

Sample Explanations

For test case 1, only one note is ever played at any given time. The maximum and minimum key number currently pressed is the same, so their difference is zero.

For test case 2, we have the following keys pressed and reach needed at each timestep:

Timestep	Keys	Reach	Timestep	Keys	Reach
1	47	0 (47 - 47)	6	32, 20	12 (32 - 20)
2	47, 32	15 (47 - 32)	7	32, 20, 51	31 (51 - 20)
3	47, 32, 20	27 (47 - 20)	8	32, 20	12 (32 - 20)
4	32, 20	12 (32 - 20)	9	20	0 (20 - 20)
5	32, 20, 44	24 (44 - 20)	10	(None)	0 (No keys)

The max reach at any timestep is 31, which occurs at step 7 while pressing keys 51, 32, and 20. The reach needed here is the largest distance between any two of the keys, 51 - 20 = 31.